

- (G1) A spacecraft of mass m and velocity \vec{v} approaches a massive planet of mass M and orbital velocity \vec{u} , as measured by an inertial observer. We consider a special case, in which the incoming trajectory of the spacecraft is designed in a way such that velocity vector of the planet does not change direction due to the gravitational boost given to the spacecraft. In this case, the gravitational boost to the velocity of the spacecraft can be estimated using conservation laws, by measuring the asymptotic velocity of the spacecraft before and after the interaction and the angle of approach of the spacecraft.

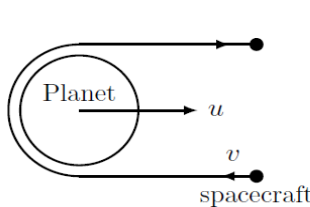


Figure 1

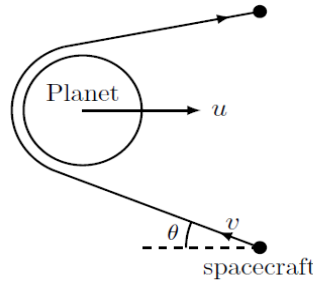


Figure 2

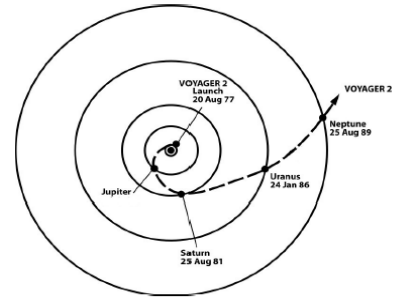


Figure 3

- (G1.1) What will be the final velocity (\vec{v}_f) of the spacecraft, if \vec{v} and \vec{u} are exactly anti-parallel (see Figure 1)? 3
- (G1.2) Simplify the expression for the case in which $m \ll M$. 1
- (G1.3) If the angle between \vec{v} and $-\vec{u}$ is θ , and $m \ll M$ (see Figure 2), use the results above to write an expression for the magnitude of the final velocity (v_f). 3
- (G1.4) The table on the last page gives data for the Voyager-2 spacecraft for a few months in the year 1979, as it passed close to Jupiter. Assume that the observer is located at the centre of the Sun. The distance from the observer is given in AU and λ is the heliocentric ecliptic longitude in degrees. Assume all objects to be in the ecliptic plane. Assume the orbit of the Earth is circular. Plot the appropriate variable against the date of observation to find the date at which the spacecraft was closest to Jupiter, and label the graph G1.4. 8
- (G1.5) Find the Earth-Jupiter distance, (d_{E-J}) on the day of the encounter. 4
- (G1.6) On the day of the encounter, around what standard time (t_{std}) had Jupiter transited the meridian in the sky of Bhubaneswar (20.27° N; 85.84° E; UT + 05:30)? 6
- (G1.7) The speed of the spacecraft (in km s^{-1}) as measured by the same observer, on some dates before the encounter and some dates after the encounter, are given below. Here, day n is the date of encounter. Use this data to find the orbital speed of Jupiter (u) on the date of the encounter and the angle θ . 12

date	n-45	n-35	n-25	n-15	n-5	n
v_{tot}	10.1408	10.0187	9.9078	9.8389	10.2516	25.5150
date	n+5	n+15	n+25	n+35	n+45	
v_{tot}	21.8636	21.7022	21.5580	21.3812	21.2365	

- (G1.8) Find the eccentricity, e_J , of Jupiter's orbit. 8
- (G1.9) Find the heliocentric ecliptic longitude, λ_p , of Jupiter's perihelion point. 5

Month	Date	λ ($^{\circ}$)	Distance (AU)
June	1	135.8870	5.1589731906
June	2	135.9339	5.1629499712
June	3	135.9806	5.1669246607
June	4	136.0272	5.1708975373
June	5	136.0736	5.1748689006
June	6	136.1200	5.1788390741
June	7	136.1662	5.1828084082
June	8	136.2122	5.1867772826
June	9	136.2582	5.1907461105
June	10	136.3040	5.1947153428
June	11	136.3496	5.1986854723
June	12	136.3951	5.2026570402
June	13	136.4405	5.2066306418
June	14	136.4857	5.2106069354
June	15	136.5307	5.2145866506
June	16	136.5756	5.2185705999
June	17	136.6202	5.2225596924
June	18	136.6647	5.2265549493
June	19	136.7090	5.2305575243
June	20	136.7532	5.2345687280
June	21	136.7970	5.2385900582
June	22	136.8407	5.2426232385
June	23	136.8841	5.2466702671
June	24	136.9273	5.2507334797
June	25	136.9702	5.2548156324
June	26	137.0127	5.2589200110
June	27	137.0550	5.2630505798
June	28	137.0969	5.2672121872
June	29	137.1384	5.2714108557
June	30	137.1795	5.2756542053
July	1	137.2200	5.2799520895
July	2	137.2600	5.2843175880
July	3	137.2993	5.2887686308
July	4	137.3378	5.2933308160
July	5	137.3754	5.2980426654
July	6	137.4118	5.3029664212
July	7	137.4467	5.3082133835
July	8	137.4798	5.3140161793
July	9	137.5116	5.3210070441
July	10	137.5628	5.3312091210
July	11	137.6898	5.3405592121
July	12	137.8266	5.3466522674
July	13	137.9599	5.3516661563
July	14	138.0903	5.3561848203
July	15	138.2186	5.3604205657
July	16	138.3453	5.3644742164

Month	Date	λ ($^{\circ}$)	Distance (AU)
July	17	138.4707	5.3684017790
July	18	138.5949	5.3722377051
July	19	138.7183	5.3760047603
July	20	138.8409	5.3797188059
July	21	138.9628	5.3833913528
July	22	139.0841	5.3870310297
July	23	139.2048	5.3906444770
July	24	139.3250	5.3942369174
July	25	139.4448	5.3978125344
July	26	139.5641	5.4013747321
July	27	139.6831	5.4049263181
July	28	139.8016	5.4084696349
July	29	139.9198	5.4120066575
July	30	140.0377	5.4155390662
July	31	140.1553	5.4190683021
August	1	140.2725	5.4225956100
August	2	140.3895	5.4261220723
August	3	140.5062	5.4296486357
August	4	140.6225	5.4331761326
August	5	140.7387	5.4367052982
August	6	140.8546	5.4402367851
August	7	140.9702	5.4437711745
August	8	141.0856	5.4473089863
August	9	141.2007	5.4508506867
August	10	141.3157	5.4543966955
August	11	141.4303	5.4579473912
August	12	141.5448	5.4615031166
August	13	141.6591	5.4650641822
August	14	141.7731	5.4686308707
August	15	141.8869	5.4722034391
August	16	142.0006	5.4757821220
August	17	142.1140	5.4793671340
August	18	142.2272	5.4829586711
August	19	142.3402	5.4865569133
August	20	142.4530	5.4901620256
August	21	142.5657	5.4937741595
August	22	142.6781	5.4973934544
August	23	142.7904	5.5010200385
August	24	142.9024	5.5046540300
August	25	143.0143	5.5082955377
August	26	143.1260	5.5119446617
August	27	143.2375	5.5156014948
August	28	143.3488	5.5192661222
August	29	143.4599	5.5229386226
August	30	143.5709	5.5266190687
August	31	143.6817	5.5303075275